

**Instructions:** Write complete legible solutions to the following problems in the space provided. Be sure to supply all the necessary steps that lead to your answers.

1. Find a parametric representation to the given surfaces
  - a. The equation of the plane that passes through  $p(1,1,-1)$  and contains the vectors  $\mathbf{u} = 2\mathbf{i} + \mathbf{j} - \mathbf{k}$ , and  $\mathbf{v} = \mathbf{i} - \mathbf{j} + 2\mathbf{k}$

- b.  $z = \sqrt{x^2 + 4y^2}$

- c. The part of the sphere  $x^2 + y^2 + z^2 = 1$  that lies below  $z = \sqrt{x^2 + y^2}$

- d. The part of the plane  $z = x + 3$  that lies inside the cylinder  $x^2 + y^2 = 1$

2. Find an equation of the tangent plane to the given parametric surface at the specified point.

$$x = u^2 + 1, y = v^3 + 1, z = u + v, p(5, 2, 3)$$

3. Find the surface area of the part of the paraboloid  $y = x^2 + z^2$  that lies inside the cylinder

$$x^2 + z^2 = 9$$

4. Find the surface area of the part of the sphere  $4 = x^2 + y^2 + (z - 2)^2$  that lies inside the cylinder

$$x^2 + y^2 = 1$$